# Supplementary - Adjoint Rigid Transform Network: Task-conditioned Alignment of 3D Shapes

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In this supplementary material we provide further details about our method such as architecture and rotation representation used in ART. Next, we provide more results for shape reconstruction and alignment using ART on ShapeNet [3]. We also provide more qualitative results for human mesh registration and pose interpolation.

# **1. Architecture Details**

In this section we describe the architecture of Adjoint Rigid Transform (ART) Network for point clouds and meshes respectively.

**Point cloud** The architecture for point cloud inputs resembles the T-net in PointNet [8]. Specifically, we first learn point-wise features by three 1D convolutional layers of size [64, 128, 1024]. A max-pooling layer then aggregates features over all points and produces a global feature vector. It is subsequently mapped to the rotation representation by three fully-connected layers with size [512, 256, 6]. We apply batch normalization [6] and ReLU to every layer except the input and output. The number of training samples in each ShapeNet category ranges from 3000 to 8000, while we train on 20000 samples for human registration.

**Mesh** For mesh inputs, we assume that they are registered to a common template and thus have the same connectivity. To keep the architecture simple, we only use mesh down-sampling layers and fully-connected layers. We first simplify the mesh to  $\frac{1}{16}$  of its original resolution based on the quadric error metrics proposed in [4]. This down-sampling rate is shown to work well for meshes parameterized by SMPL [7], but it might need to be tuned on other meshes. Then we flatten the down-sampled mesh and feed it to fully-connected layers of size [128, 64, 6]. Human pose transfer is trained on 120000 samples.

## 2. Rotation Representation

We choose to use the continuous rotation representation proposed by Zhou *et al.* [10] since it was shown to be superior to other representations such as quaternions and Euler angles in rotation regression tasks. Let  $R_A$  be a learnable function. We have

$$[\boldsymbol{a}_1 \ \boldsymbol{a}_2] = R_A \left( \mathbf{X} \right) \tag{1}$$

where  $a_1$  and  $a_2$  are vectors in  $\mathbb{R}^3$ . Then we apply Gram-Schmidt process to obtain the orthogonal matrix **R**.

$$\mathbf{R} = [\boldsymbol{r}_1 \ \boldsymbol{r}_2 \ \boldsymbol{r}_3] \tag{2}$$

$$= \left[ \frac{a_1}{\|a_1\|} \frac{a_2 - (a_2^T r_1) r_1}{\|a_2 - (a_2^T r_1) r_1\|} r_1 \times r_2 \right]$$
(3)

Note that in the last column of  $\mathbf{R}$  we take cross product of the first two columns to ensure det $(\mathbf{R}) = 1$ .

# 3. Scale Alignment

Besides orientation alignment, we can also extend ART to align the scale of shapes by predicting a scaling factor for each input shape, and enforcing scaling equivariance in the same manner as rotation equivariance. The new equivariance constraint then becomes

$$S_{A}(\boldsymbol{X}) R_{A}(\boldsymbol{X}) \boldsymbol{X} = sS_{A}(s\boldsymbol{R}\boldsymbol{X}) R_{A}(s\boldsymbol{R}\boldsymbol{X}) \boldsymbol{R}\boldsymbol{X},$$
(4)

where  $s \in \mathbb{R}^+$ ,  $\mathbf{R} \in SO(3)$  are random scaling factor and rotation,  $S_A$  and  $R_A$  perform scaling and rotation canonicalization respectively. We trained the extended model on the SMAL [11] dataset and example alignment results are shown in Fig. 1.

# 4. Shape Alignment

We show the distribution curves of pairwise alignment error for all categories under random azimuthal rotation



Figure 1. Top: Input SMAL shapes from five different categories. Bottom: ART-aligned shapes with consistent orientations and scales.



Figure 2. Percentage of shape pairs with an angular distance less than the given thresholds.



Figure 3. Effect of data perturbation on alignment.

in Fig. 2. Since the table category suffers from ambiguity of rotation symmetry, the quantitative measure on tables is not conclusive and we only include it here for completeness. We can observe that the alignment accuracy for planes, chairs and sofas are good, with more than 80% of shape pairs differing by less than 30°. However, ART was still confused by the front and back of cars and learned two modes of canonical orientations, as can be seen from the blue curve. Qualitative results for random 3D alignment are demonstrated in Fig. 4.

Shapes captured from real world sensor data are often accompanied with noise and holes. Hence we also evaluate the robustness of ART alignment to various shape perturbations. We apply random Gaussian noise with different standard deviation  $\sigma$  as an approximation of real noise. To simulate holes, we randomly sample a given number of points from the point cloud as hole centers, and remove all points within a radius of 0.2 from the centers. The alignment error distribution plot is shown in Fig. 3. ART is robust to a reasonable amount of noise and holes. Even in the worst case the alignment accuracy is comparable to PCA (see Fig. 7 in main paper).

# 5. Point Cloud Auto-encoding

ART improves the performance of existing methods [1] on point cloud reconstruction by aligning the data to a common global orientation. We show more qualitative examples for point cloud reconstruction using ART in Fig. 5.

#### 6. Human Body Registration

We show more qualitative examples for human mesh registration using ART in Fig. 6. This experiment clearly highlights the general applicability of ART for non-rigid objects. It can also be seen that human meshes with varying poses can still be aligned to a common global orientation with ART.

# 7. Human Pose Interpolation

The human pose interpolation method used by Zhou *et al.* [9] can have squeezing artifacts when the source and the

target differs by a nontrivial global rotation. ART mitigates this problem by explicitly factoring out and interpolating global rotations. Additional qualitative results are shown in Fig. 7.

## 8. Limitations and Future Work

ART is a simple yet effective module that helps a wide variety of 3D networks to achieve satisfactory performance when training on data without pre-alignment. However, it can still be improved in several aspects. First, although the formulation of ART subsumes general rotations in SO(3), currently it performs much better on shapes perturbed by random azimuthal rotations only. We hypothesize that this limitation is related to architecture capacity. Hence we plan to explore using SotA point cloud architectures as the backbone of ART. Besides, ART learns semantic features for shape alignment completely from scratch. In future work, we plan to utilize more geometric properties such as the plane of reflection so that ART can have more clues to make accurate predictions.

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Figure 4. Alignment of shapes perturbed by random 3D rotations with ART. The last column shows failure cases.



Figure 5. Reconstruction of ShapeNet surfaces with ART. We show the groundtruth surfaces, surfaces aligned by ART, and point cloud reconstructions in order.



Figure 6. Registration of (rotated) raw FAUST [2] scans using 3D-CODED [5] and ART. Note that all results were obtained using single initialization.



Figure 7. Human pose interpolation using Zhou *et al.* [9]. The source pose is at s = 0 and target pose at s = 1. We show three intermediate poses at uniform time steps.